

GAN

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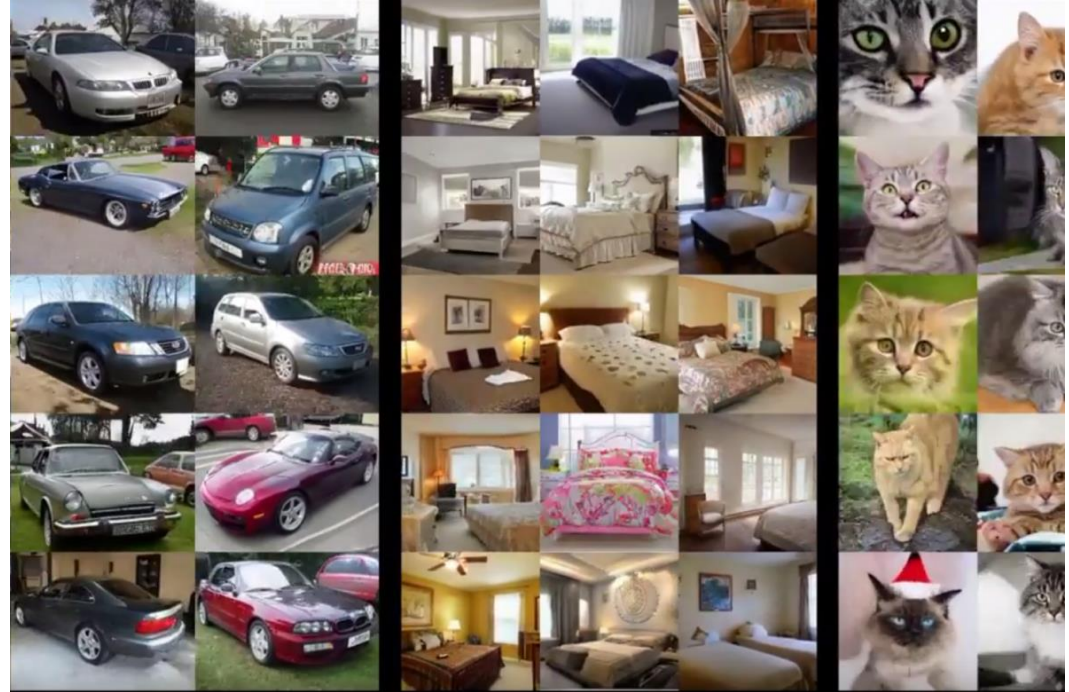
고재필

Generative-Adversarial Networks

- 대립(Adversarial) 방식을 통해 (학습하는) 생성적(Generative) 신경망

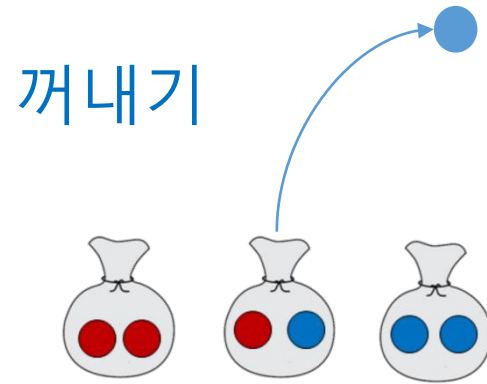


Google (2017)

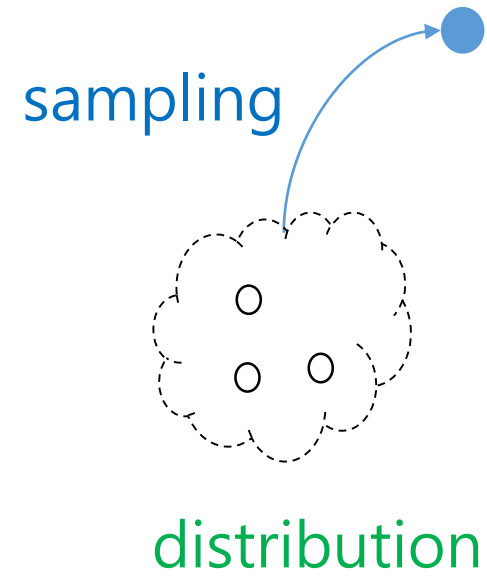


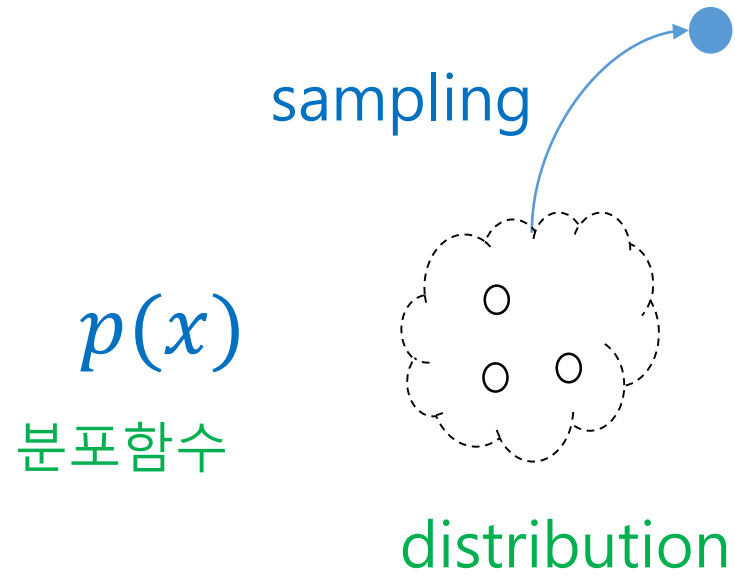
NVidia (2019)

들어가기...

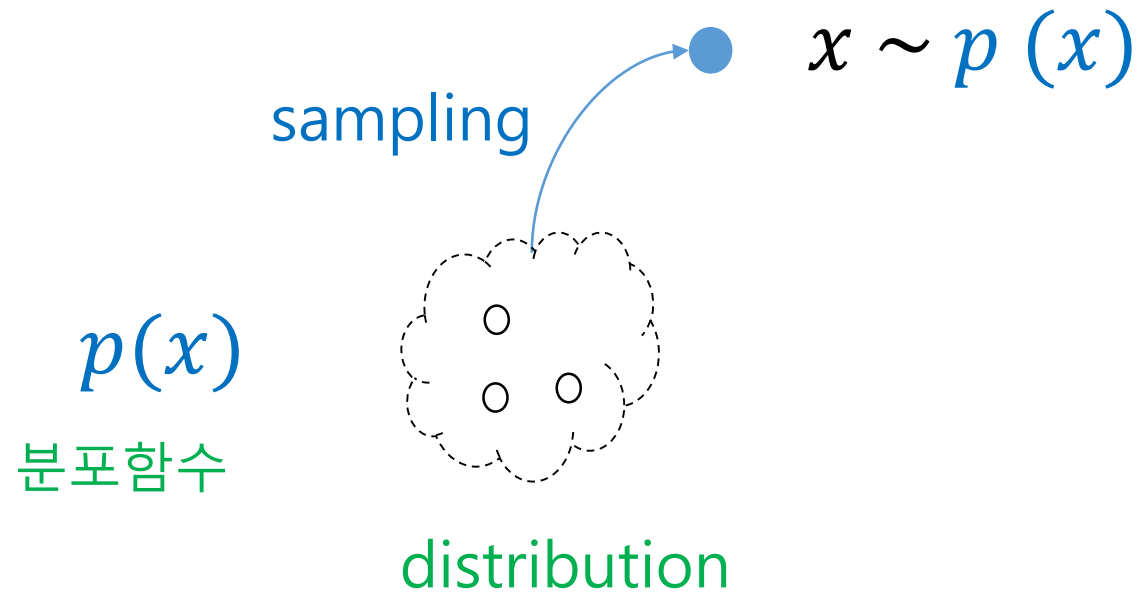


'어느 주머니'인지에 따라
꺼내 온 구슬이 달라진다.

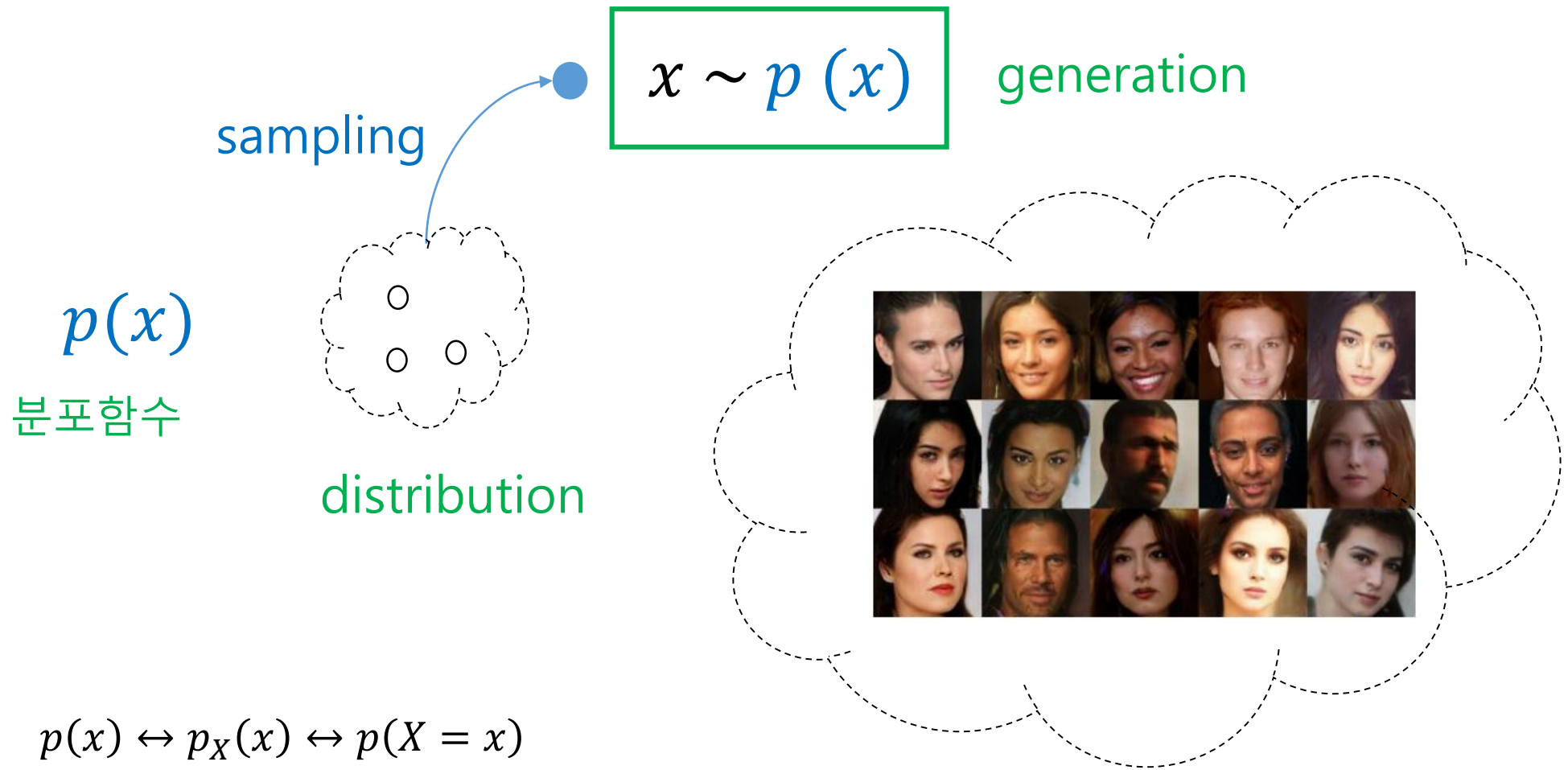




$$p(x) \leftrightarrow p_X(x) \leftrightarrow p(X = x)$$



$$p(x) \leftrightarrow p_X(x) \leftrightarrow p(X = x)$$



information $-\log p(x)$

expectation $E[X] = \sum_x xp(x)$

$$E[f(X)] = \sum_x f(x)p(x)$$

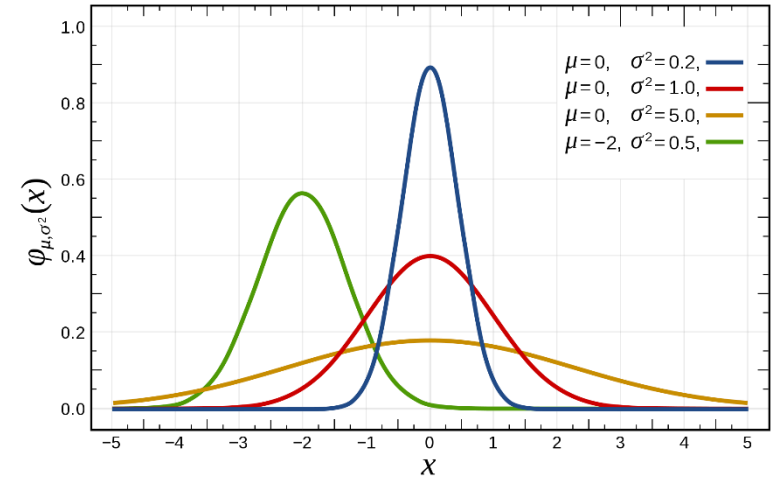
entropy $E[-\log p(x)] = \sum_x -\log p(x)p(x)$

Bayes' rule $p(y|x) = \frac{p(x,y)}{p(x)} = \frac{p(y)p(x|y)}{\sum_y p(y)p(x|y)}$

$$p(x,y) = p(x)p(y|x) = p(y)p(x|y)$$

$$p(x,y,z) = p(x)p(y|x)p(z|x,y)$$

$$p(x) = \sum_y p(x,y) = \sum_y p(y)p(x|y)$$



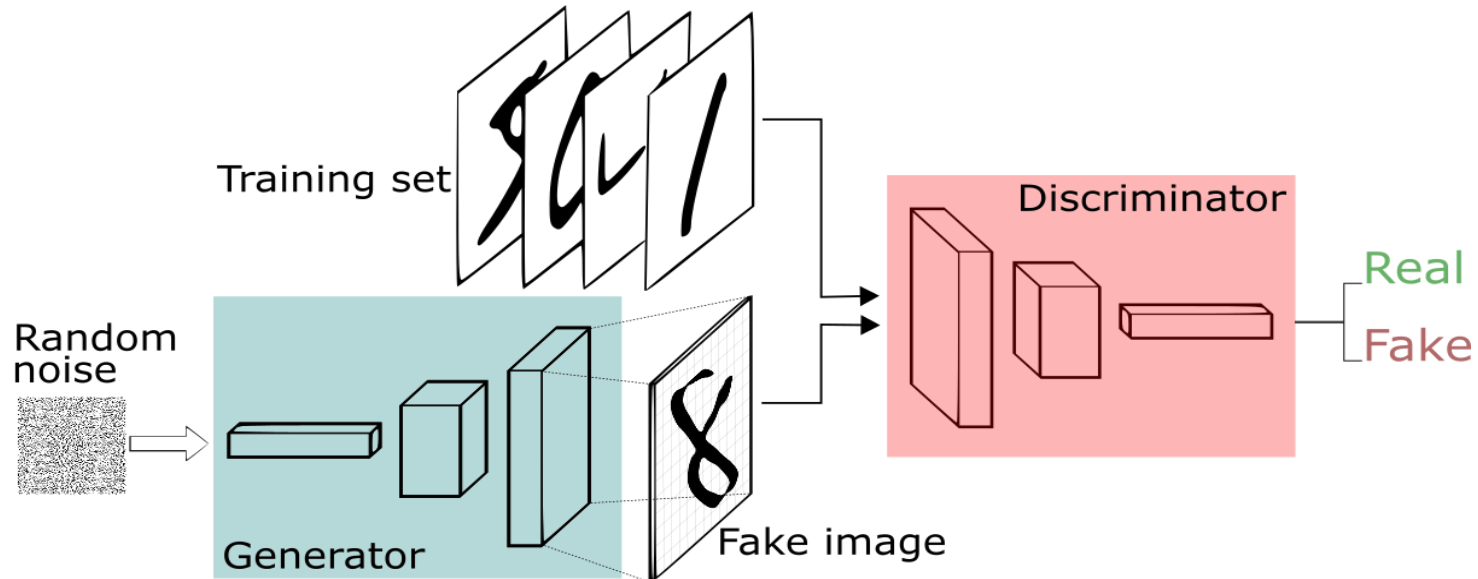
$$p(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$

$$p(x; u, \sigma)$$

$$p_{\theta}(x) \quad \theta = (u, \sigma)$$

신경망 구조

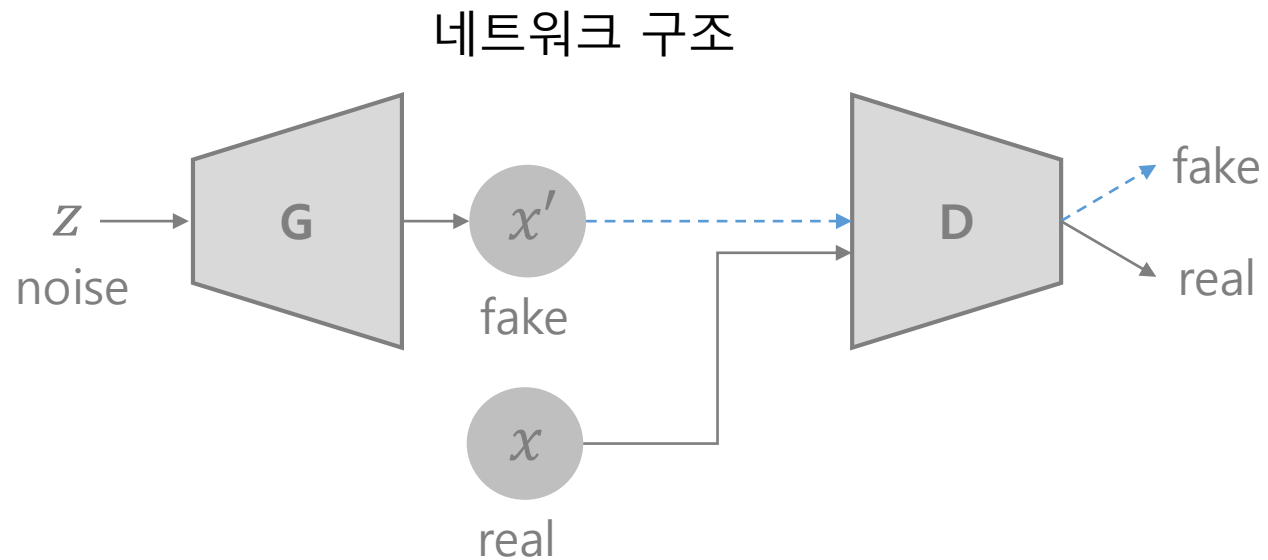
- 대립(Adversarial) 방식을 통해 학습하는 생성적(Generative) 신경망
- 생성자(**G**enerator)와 구분자(**D**iscriminator)가 대립하는 네트워크 구조
adversarial



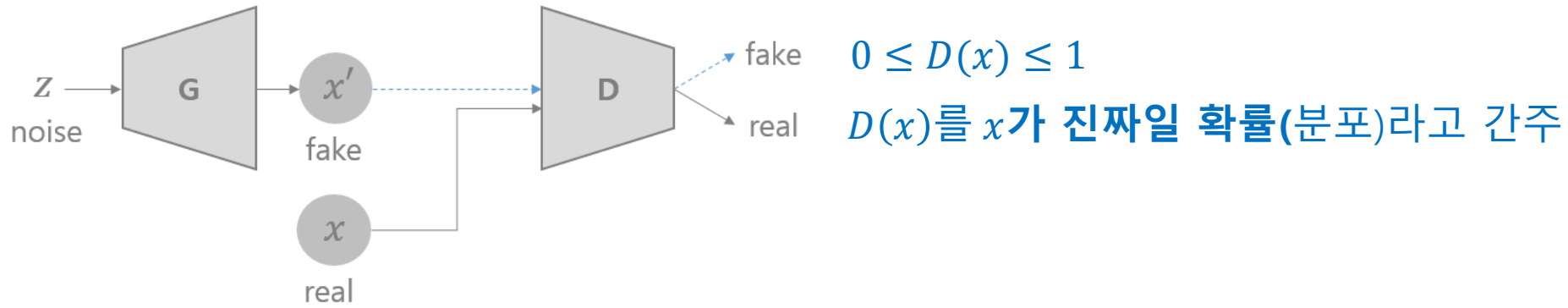
생성자의
손실함수 역할

손실함수

- 목적함수
 - 생성자(G)는 진짜 같은 데이터를 생성하고,
 - 구분자(D)는 진짜 데이터와 생성된 데이터를 잘 구분하도록,
 - 학습하는 것을 목적으로 해야 한다.



목적함수 ?



- ① 우리의 목표는 진짜인 x 에 대해서 $D(x)$ 를 커지게 하고 합성된 녀석인 $x' = G(z)$ 에 대해서 $D(G(z))$ 가 작아지도록 하는 것이다.

$$\max D(x)$$

$$\max (1 - D(G(z)))$$

$D(G(z))$ 를 최소화하는 것을
 최대화 하는 식으로 바꾼 것

$$\max D(x) + (1 - D(G(z)))$$

이 식을 최대화 하자

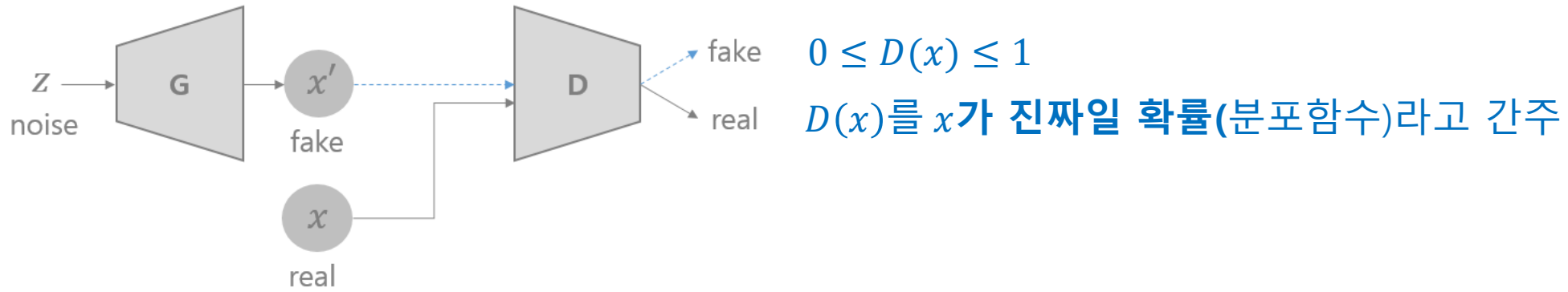
결론적으로 다음과 같이 표현할 수 있다.

$$\min_G \max_D D(x) + (1 - D(G(z)))$$

- ② 그리고, $D(G(z))$ 가 1이 되도록 한다.

$$\max D(G(z))$$

$$\min (1 - D(G(z)))$$



- ① 우리의 목표는 진짜인 x 에 대해서 $D(x)$ 를 커지게 하고 합성된 녀석인 $x' = G(z)$ 에 대해서 $D(G(z))$ 가 작아지도록 하는 것이다.

$$\left. \begin{array}{l} \max D(x) \\ \max (1 - D(G(z))) \end{array} \right\} \max \frac{D(x) + (1 - D(G(z)))}{2}$$

이 식을 최대화 하자

이 값을 최소화

서로 상충

결론적으로 다음과 같이 표현할 수 있다.

$$\min_G \max_D D(x) + (1 - D(G(z)))$$

- ② 그리고, $D(G(z))$ 가 1이 되도록 한다.

$$\begin{array}{l} \max D(G(z)) \\ \min (1 - D(G(z))) \end{array}$$

동시에 만족시킬 수 없다.
 번갈아 가며 최대화/최소화를 해야 한다.

목적함수

$$\min_G \max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(1 - D(G(\mathbf{z})))]$$

D에 log 취해도 무방-대소관계유지, 그리고 값 하나보단 평균이 낫다.

$$\max D(x) + (1 - D(G(z)))$$

$$\max D(G(z)) \text{ 최대화 식}$$

$$\min (1 - D(G(z))) \text{ 최소화 식}$$

손실함수

$$\text{Loss}D = - \left(\mathbb{E}_{x \sim p_{\text{data}}(x)} [\log D(x)] + \mathbb{E}_{z \sim p_z(z)} [\log (1 - D(G(z)))] \right)$$

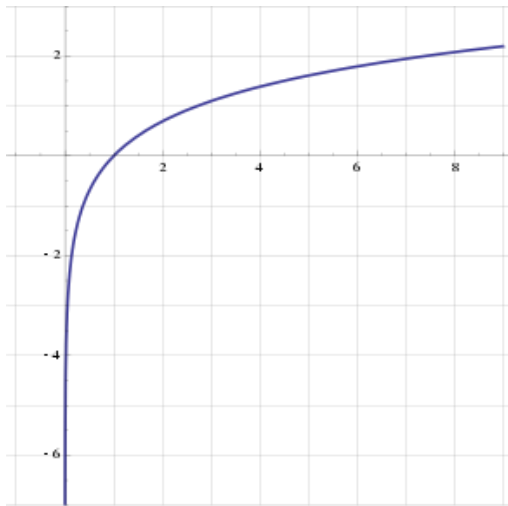
$$\text{Loss}G = \mathbb{E}_{z \sim p_z(z)} [\log (1 - D(G(z)))]$$

$$\text{Loss}G = -\mathbb{E}_{z \sim p_z(z)} [\log D(G(z))] \text{ 선호}$$

$$LossG = E_{z \sim p_z(z)} \left[\log \left(1 - D(G(z)) \right) \right]$$

$$LossG = -E_{z \sim p_z(z)} \left[\log D(G(z)) \right]$$

$$LossG = 1 - E_{z \sim p_z(z)} \left[\log D(G(z)) \right]$$

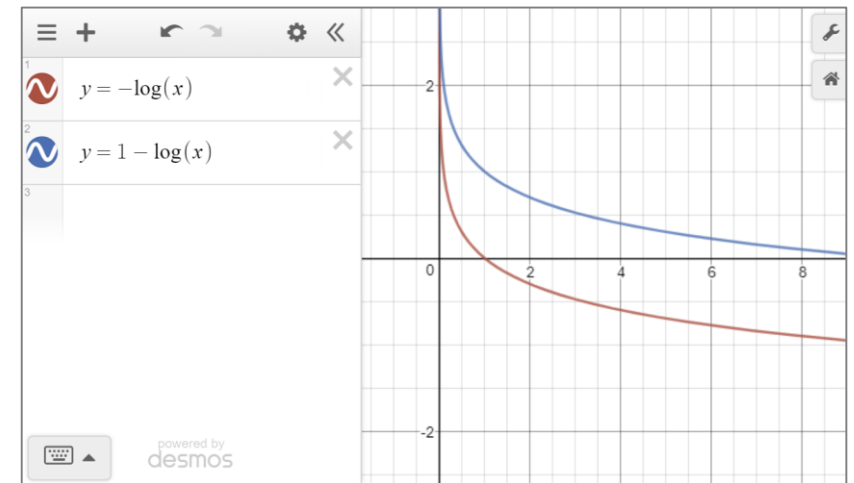


학습 초기에는
G가 만들어내는 결과가 형편 없음
→ D가 거의 0일 가능성이 높음.

$\log(1-D)$,
 $\log(1)$ 근방에서는 기울기가 작다.

$\log(D)$,
 $\log(0)$ 근방에서는 기울기가 크다.

+1을 해서 최소가 0이 되도록 하여 사용
(그림에서 파란색 그래프)



<https://www.desmos.com/calculator>

Algorithm 1 Minibatch stochastic gradient descent training of generative adversarial nets. The number of steps to apply to the discriminator, k , is a hyperparameter. We used $k = 1$, the least expensive option, in our experiments.

for number of training iterations **do**

for k steps **do**

- Sample minibatch of m noise samples $\{z^{(1)}, \dots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Sample minibatch of m examples $\{x^{(1)}, \dots, x^{(m)}\}$ from data generating distribution $p_{\text{data}}(x)$.
- Update the discriminator by ascending its stochastic gradient:

최대값 구하기이므로,
그레디언트의 + 방향으로 업데이트

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[\log D(x^{(i)}) + \log \left(1 - D(G(z^{(i)})) \right) \right].$$

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \dots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Update the generator by descending its stochastic gradient:

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log \left(1 - D(G(z^{(i)})) \right).$$

최소값 구하기이므로,
그레디언트의 - 방향으로 업데이트

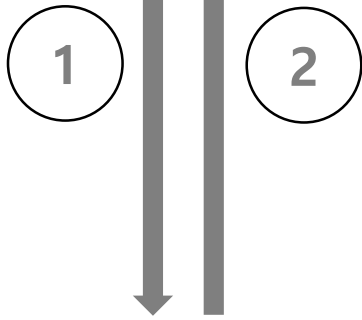
end for

The gradient-based updates can use any standard gradient-based learning rule. We used momentum in our experiments.

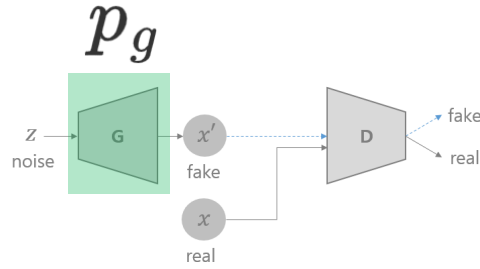
update D
for a fixed G

최적화 목적을 달성하면...

$$p_g = p_{\text{data}}$$



$$D(x) = \frac{1}{2}$$



G가 실제 data 분포를 완벽하게 나타내어, D가 구분 못하는 상황

1/2 이 나오는지 보자

$$\min_G \max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(1 - D(G(\mathbf{z})))]$$

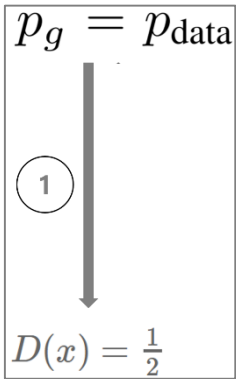
일단 G가 구해졌다고 가정하고, 목적함수를 최대화하는 D를 먼저 구해보자.

$$\max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(1 - D(G(\mathbf{z})))]$$

$$x = G(z)$$

$$= \int_{\mathbf{x}} p_{\text{data}}(\mathbf{x}) \log(D(\mathbf{x})) dx + \int_{\mathbf{z}} p_{\mathbf{z}}(\mathbf{z}) \log(1 - D(G(\mathbf{z}))) dz$$

z를 없애자



$$= \int_{\mathbf{x}} p_{\text{data}}(\mathbf{x}) \log(D(\mathbf{x})) dx + \int_{\mathbf{z}} p_{\mathbf{z}}(\mathbf{z}) \log(1 - D(\mathbf{x})) dz$$

$$x = G(z)$$

$$\Rightarrow z = G^{-1}(x)$$

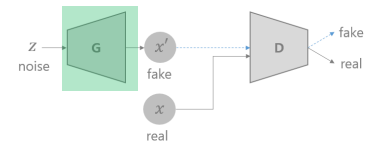
$$\Rightarrow \frac{d}{dx} z = \frac{d}{dx} G^{-1}(x)$$

$$\Rightarrow \frac{d}{dx} z = (G^{-1})'(x)$$

$$\Rightarrow dz = (G^{-1})'(x) dx$$

$$= \int_{\mathbf{x}} p_{\text{data}}(x) \log(D(x)) dx + \int_{\mathbf{x}} p_{\mathbf{z}}(G^{-1}(x)) \log(1 - D(x)) (G^{-1})'(x) dx$$

$$p_g(x) \equiv p_{\mathbf{z}}(G^{-1}(x)) (G^{-1})'(x)$$



$$= \int_{\mathbf{x}} p_{\text{data}}(x) \log(D(x)) dx + \int_{\mathbf{x}} p_g(x) \log(1 - D(x)) dx$$

$$E_{x \sim p_{\text{data}}}[\log(D(x))]$$

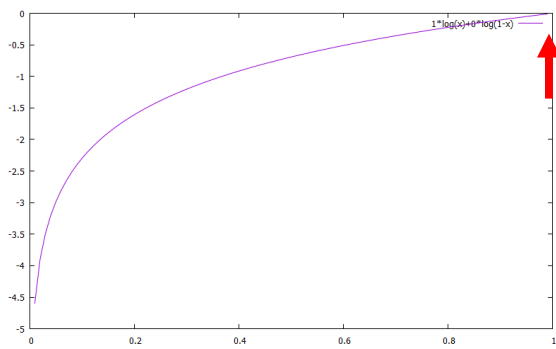
$$E_{x \sim p_g}[\log(1 - D(x))]$$

$\int_x p_{data}(x)\log(D(x)) + p_g(x)\log(1 - D(x))dx$ 이 식을 최대화하는 D를 구하고 있었다.

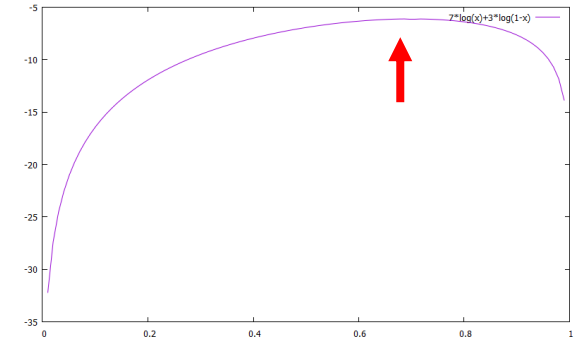
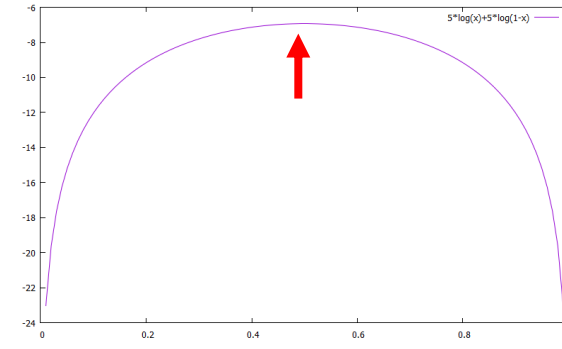
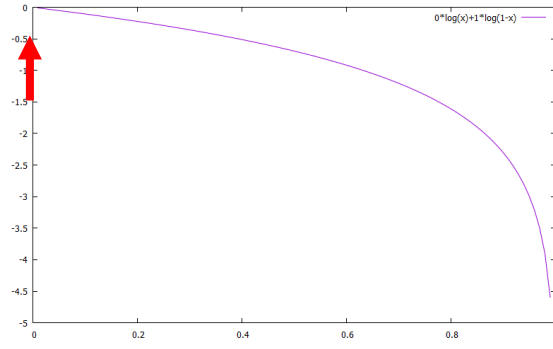
위 식의 특성을 살펴보기 좋게 대치

$$= \int a \cdot \log(y) + b \cdot \log(1 - y)dx$$

이 식의 그래프 모양은 아래와 같음



0 y 1



미분해서 0되는 지점이 최대 값

$$V(G^{fixed}, D) = a \cdot \log(y) + b \cdot \log(1 - y)$$

D; y에 대해 미분해서 0되는 지점이 최대 값

$$\frac{a}{y} + \frac{b \cdot (-1)}{1 - y} = 0 \Rightarrow a(1 - y) - by = 0 \Rightarrow y = \frac{a}{a + b}$$

$$D_G^*(\mathbf{x}) = \frac{p_{data}(\mathbf{x})}{p_{data}(\mathbf{x}) + p_g(\mathbf{x})}$$

any given G

Optimal Discriminator

$$C(G) = \max_D V(G, D)$$

$$= \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}} [\log D_G^*(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_z} [\log(1 - D_G^*(G(\mathbf{z})))]$$

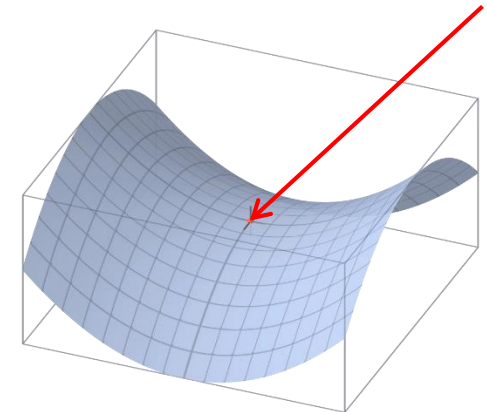
$$= \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}} [\log D_G^*(\mathbf{x})] + \mathbb{E}_{\mathbf{x} \sim p_g} [\log(1 - D_G^*(\mathbf{x}))]$$

$$= \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}} \left[\log \frac{p_{\text{data}}(\mathbf{x})}{p_{\text{data}}(\mathbf{x}) + p_g(\mathbf{x})} \right] + \mathbb{E}_{\mathbf{x} \sim p_g} \left[\log \frac{p_g(\mathbf{x})}{p_{\text{data}}(\mathbf{x}) + p_g(\mathbf{x})} \right]$$

$$D_G^*(\mathbf{x}) = \frac{p_{\text{data}}(\mathbf{x})}{p_{\text{data}}(\mathbf{x}) + p_g(\mathbf{x})} = \frac{1}{2}$$

$$p_g = p_{\text{data}}$$

$$C(G) = \log \frac{1}{2} + \log \frac{1}{2} = -\log 4$$



- **Kullback-Leibler divergence**

$$KL(p||q) = - \int p(x) \ln q(x) dx - \left(- \int p(x) \ln p(x) dx \right) = - \int p(x) \ln \left(\frac{q(x)}{p(x)} \right) dx$$

p(x)에 대한 q(x)의 엔트로피 *p(x)에 대한 p(x)의 엔트로피*

$$KL(p||q) \geq 0$$

$$KL(p||q) \neq KL(q||p)$$

$p_g = p_{\text{data}}$ 인지 보자

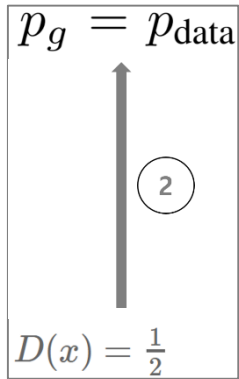
$$C(G) = \max_D V(G, D)$$

$$= \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}} [\log D_G^*(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_z} [\log(1 - D_G^*(G(\mathbf{z})))]$$

$$= \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}} [\log D_G^*(\mathbf{x})] + \mathbb{E}_{\mathbf{x} \sim p_g} [\log(1 - D_G^*(\mathbf{x}))]$$

$$= \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}} \left[\log \frac{p_{\text{data}}(\mathbf{x})}{p_{\text{data}}(\mathbf{x}) + p_g(\mathbf{x})} \right] + \mathbb{E}_{\mathbf{x} \sim p_g} \left[\log \frac{p_g(\mathbf{x})}{p_{\text{data}}(\mathbf{x}) + p_g(\mathbf{x})} \right] \quad -\log(4) + \log(4)$$

$$= -\log(4) + \int p_{\text{data}} \cdot \log \frac{p_{\text{data}}}{p_{\text{data}} + p_g} dx + \int p_g \cdot \log \frac{p_g}{p_{\text{data}} + p_g} dx$$



$$= -\log(4) + \int p_{\text{data}} \cdot \log \frac{p_{\text{data}}}{\frac{p_{\text{data}} + p_g}{2}} dx + \int p_g \cdot \log \frac{p_g}{\frac{p_{\text{data}} + p_g}{2}} dx$$

$$D_{\text{KL}}(P||Q) = \int_{-\infty}^{\infty} p(x) \log \frac{p(x)}{q(x)} dx$$

$$= -\log(4) + \left(KL \left(p_{\text{data}} \left\| \frac{p_{\text{data}} + p_g}{2} \right. \right) + KL \left(p_g \left\| \frac{p_{\text{data}} + p_g}{2} \right. \right) \right)$$

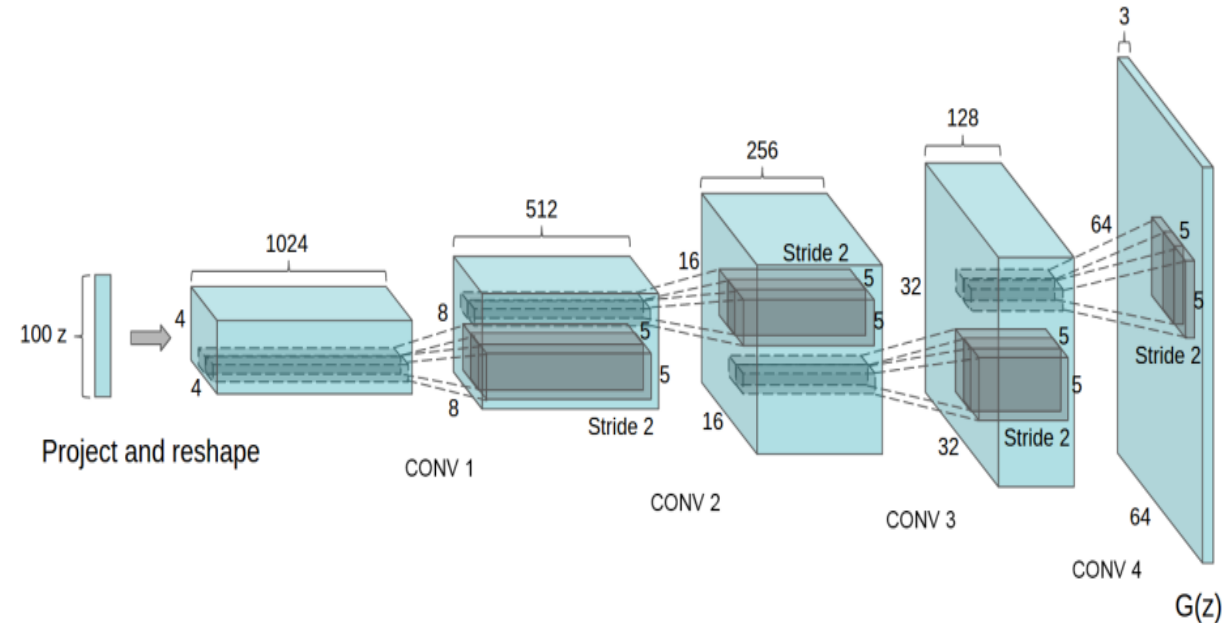
$$C(G) = -\log(4) + 2 \cdot JSD(p_{\text{data}} || p_g)$$

정의

Jensen–Shannon divergence (symmetric KL)
non-negative and **zero** only when they are equal

목적함수가
최소가 되려면 $\Rightarrow p_g = p_{\text{data}}$

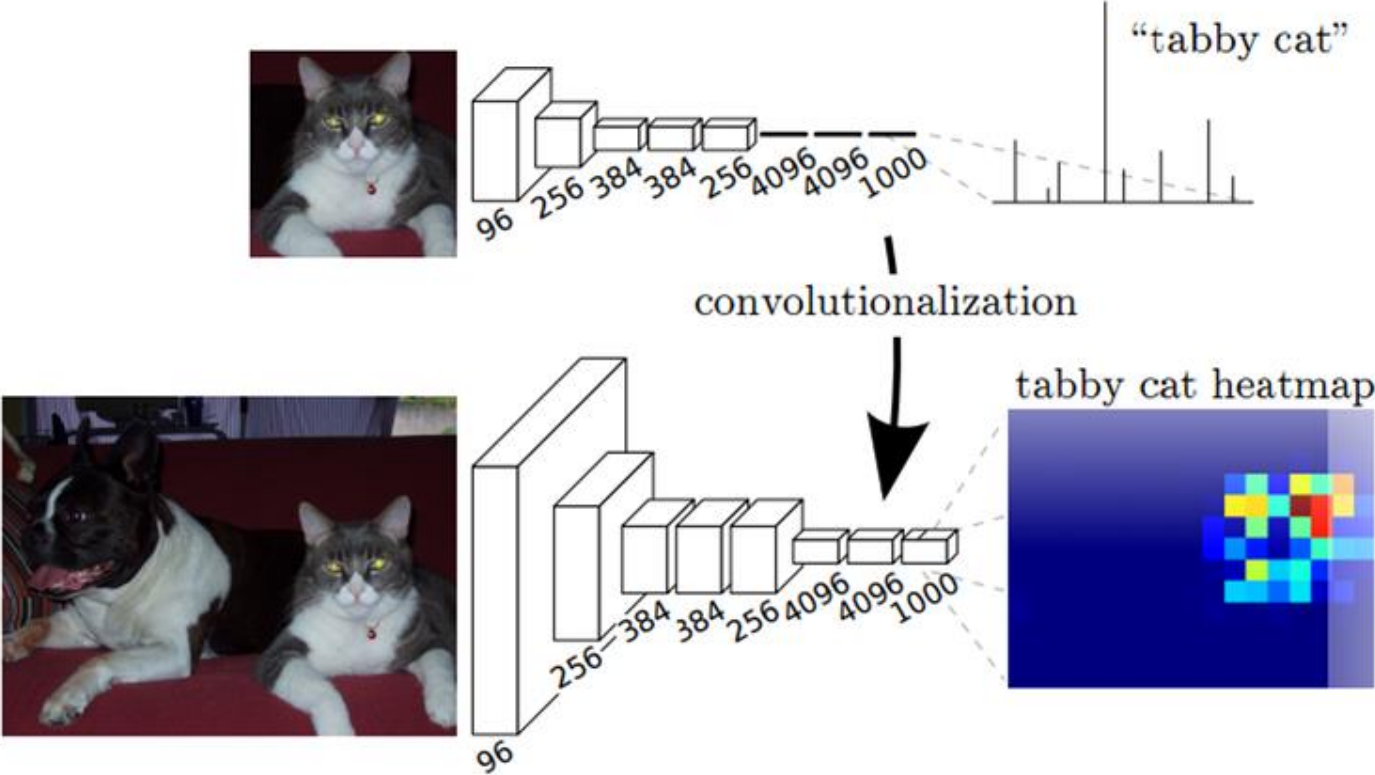
DCGAN Deep Convolutional GANs



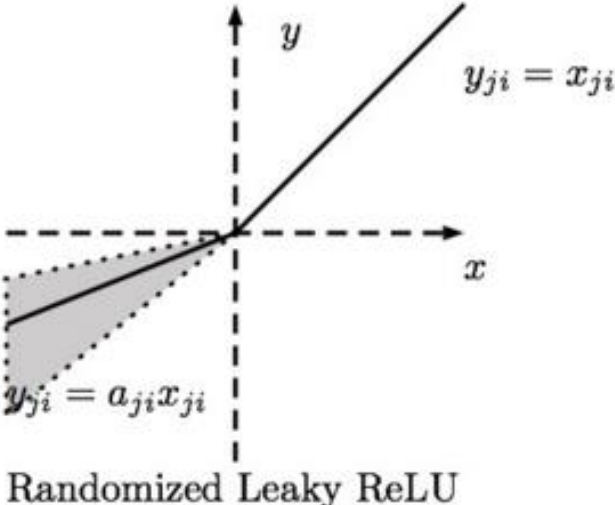
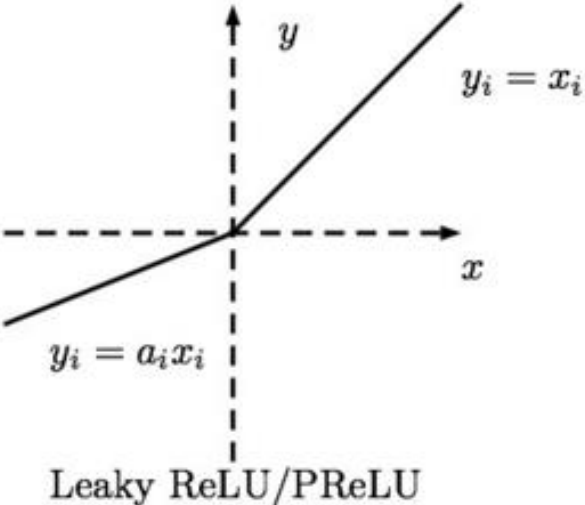
Architecture guidelines for stable Deep Convolutional GANs

- Replace any pooling layers with strided convolutions (discriminator) and fractional-strided convolutions (generator).
- Use batchnorm in both the generator and the discriminator.
- Remove fully connected hidden layers for deeper architectures.
- Use ReLU activation in generator for all layers except for the output, which uses Tanh.
- Use LeakyReLU activation in the discriminator for all layers.

Fully-Convolutional Neural Networks



Leaky ReLU



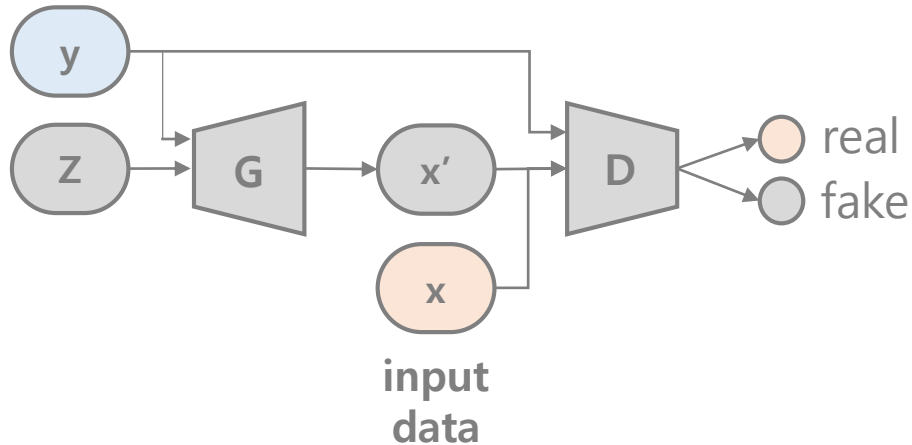
https://blog.csdn.net/cyh_24/article/details/50593400

Conditional GAN

클래스 정보를 주어서 학습하자.
특정 클래스를 생성할 수 있게 된다.

조건 정보를 제공
예들 들면, x 는 숫자영상
 y 는 그 숫자의 값, 그러면 y 에 해당되는 x' 가 생성된다.
이전 방식은 어떤 숫자의 x' 가 생성될지 모름

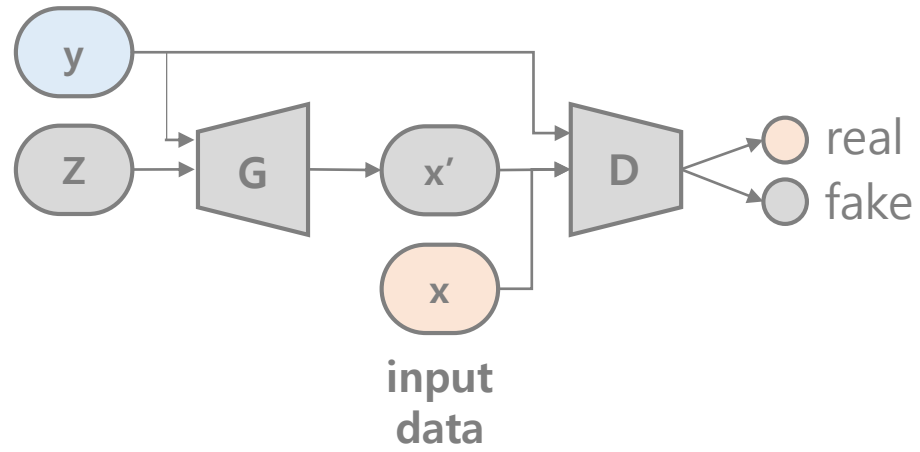
condition



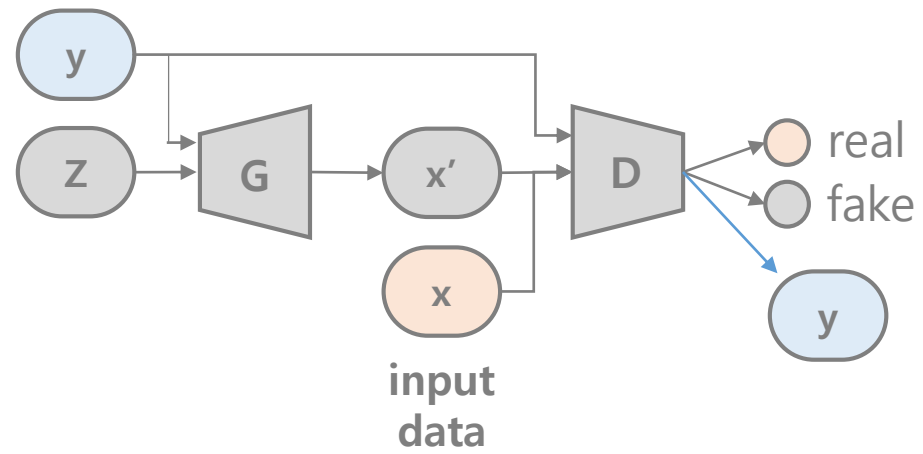
“사람이 알고 있는 정보를 제공하여,
신경망의 학습부담을 줄여준다.”

$$\min_G \max_D V(D, G) = E_{x \sim p_{data}(x)} [\log D(x, y)] + E_{z \sim p_z(z)} [\log \{1 - D(G(z, y), y)\}]$$

condition

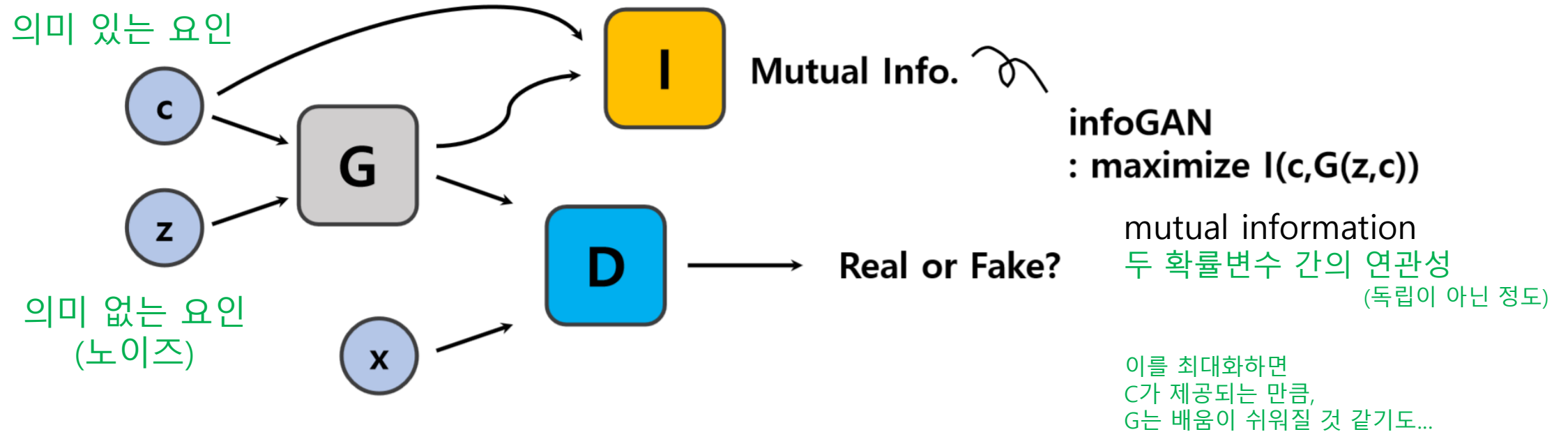


condition



InfoGAN

- 의미 있는 잠재요인(latent variable)을 네트워크가 추출하도록 구성



$$\min_G \max_D V_I(D, G) = V(D, G) - \lambda I(c; G(z, c))$$

Mutual Information

정의 $I(X; Y) = \sum_{x,y} p(x, y) \log \frac{p(x, y)}{p(x)p(y)}$ 독립이 아닌 정도에 대한 평균

$$= \sum_{x,y} p(x, y) \log \frac{p(x, y)}{p(x)} - \sum_{x,y} p(x, y) \log p(y)$$

$$= \sum_{x,y} p(x)p(y|x) \log p(y|x) - \sum_{x,y} \log p(y)p(x, y)$$

$$= \sum_x p(x) \left(\sum_y p(y|x) \log p(y|x) \right) - \sum_y \log p(y) \left(\sum_x p(x, y) \right)$$

$$= - \sum_x p(x) H(Y|X = x) - \sum_y p(y) \log p(y)$$

$$= -H(Y|X) + H(Y) \text{ 엔트로피}$$

$$= H(Y) - H(Y|X). \text{ 다른 변수로부터 얻을 수 있는 엔트로피 (평균 정보량)}$$

엔트로피가 크다는 얘기는 가능성이 낮다 (불확실성이 크다)

Y불확실성 - X가 주어졌을 때의 Y불확실성은 X가 주어져서 사라지는 불확실성

상호정보 최대화

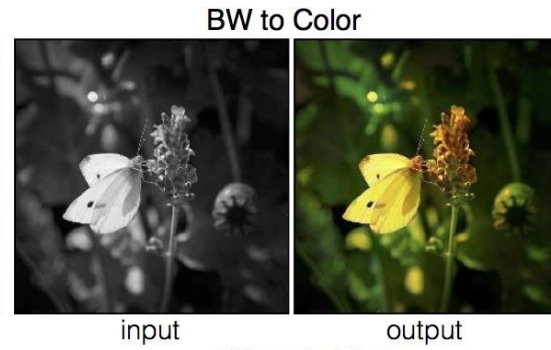
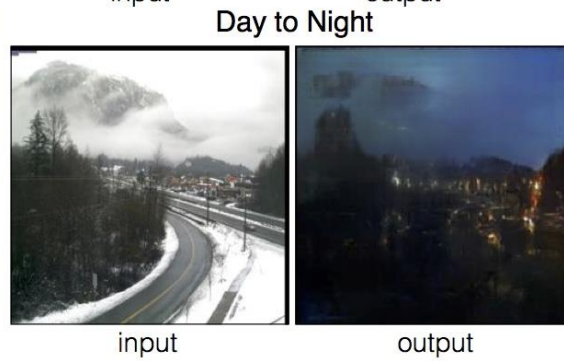
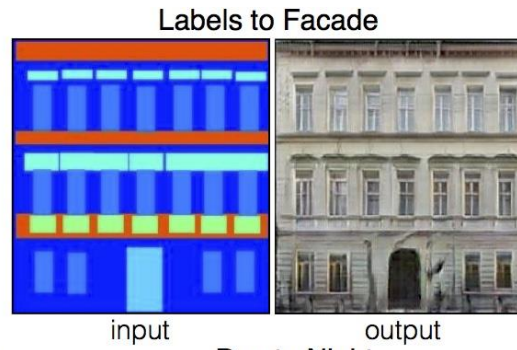
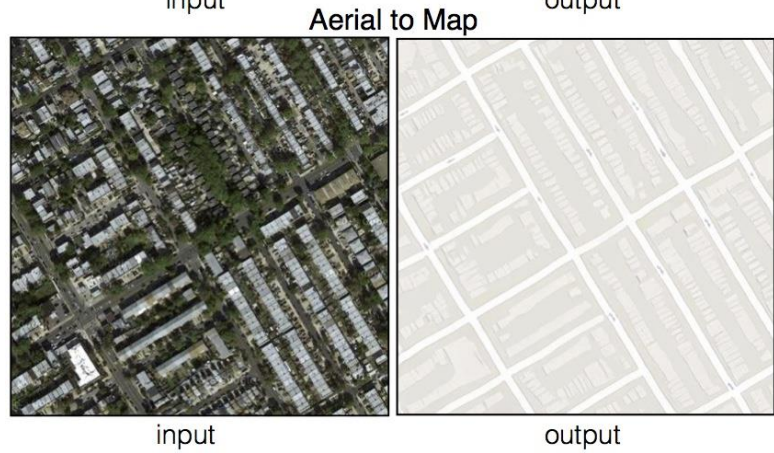
$$\begin{aligned} I[X, Y] &= H[Y] - \mathbb{E}_x H[Y|X = x] \\ &= H[Y] + \mathbb{E}_x \mathbb{E}_{y|x} \log p(y|x) \\ &= H[Y] + \mathbb{E}_x \mathbb{E}_{y|x} \log \frac{p(y|x)q(y|x)}{q(y|x)} \\ &= H[Y] + \mathbb{E}_x \mathbb{E}_{y|x} \log q(y|x) + \mathbb{E}_x \mathbb{E}_{y|x} \log \frac{p(y|x)}{q(y|x)} \\ &= H[Y] + \mathbb{E}_x \mathbb{E}_{y|x} \log q(y|x) + \mathbb{E}_x KL[p(y|x) || q(y|x)] \\ &\geq \underline{H[Y] + \mathbb{E}_x \mathbb{E}_{y|x} \log q(y|x)} \end{aligned}$$

Lower Bound

$q(y|x; \psi)$ is a parametric probability distribution

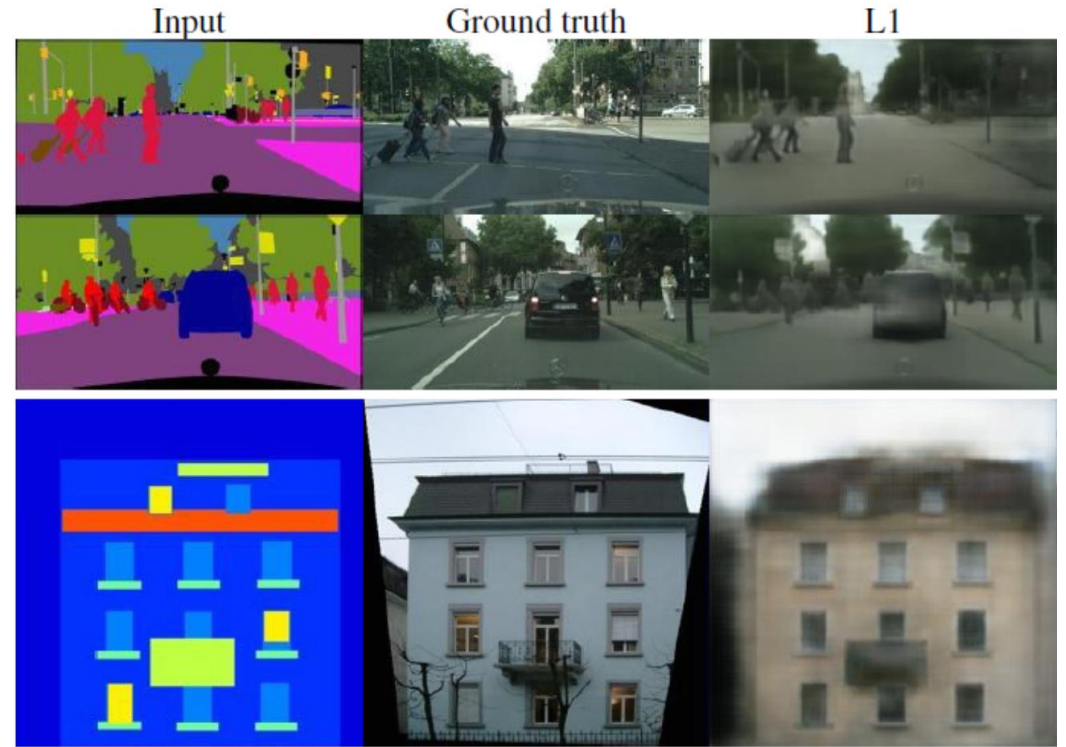
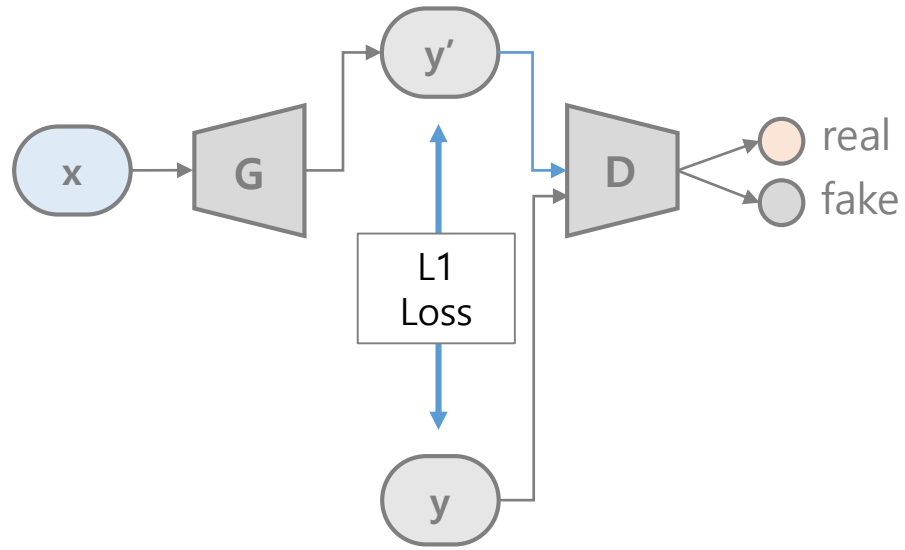
p 대신 우리가 다룰 수 있는 분포함수로 대체했음

Pix2Pix



Colorful Image
Colorization(ECCV2016)
형태유지(색깔만 변경)
데이터 취득 쉽다.

GAN + L1

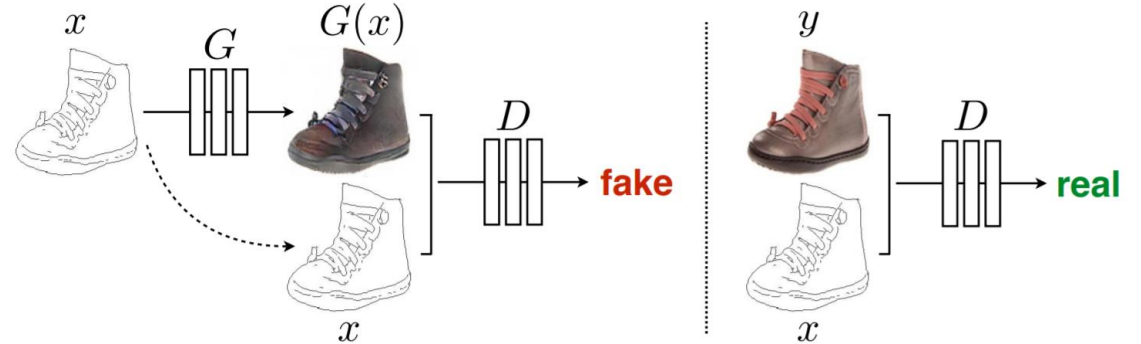
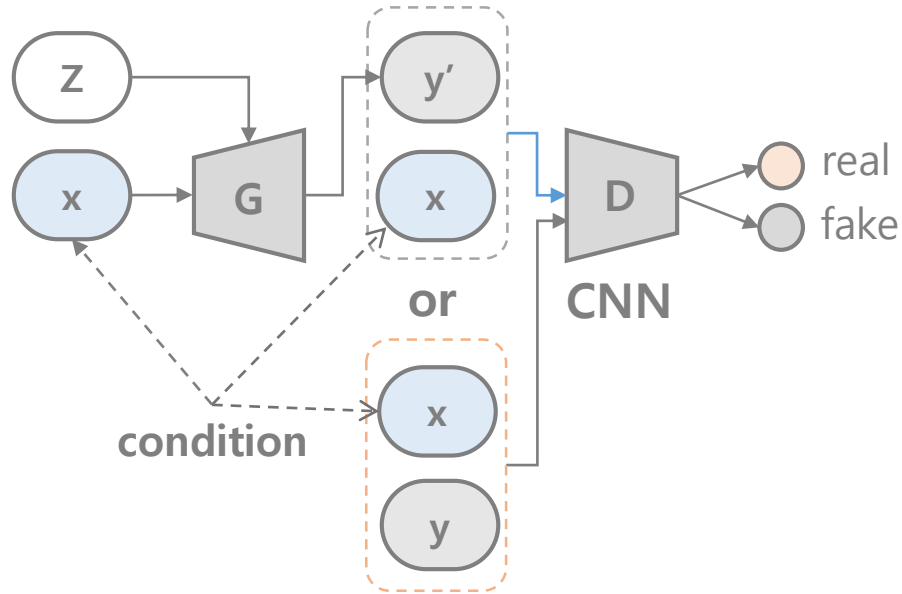


$$Loss = \sum_{x \in \text{EveryPixel}} \|GT(x) - Pred(x)\|$$

L1 loss만으로는 형태유지가 어렵다.
합(평균)관점 학습

$$\min_G \max_D \mathbb{E}_y [\log(D(y))] + \mathbb{E}_x [\log(1 - D(G(x)))] + \mathbb{E}_{x,y} [\|y - G(x)\|_1]$$

Conditional GAN + L1



$$G^* = \arg \min_G \max_D \mathcal{L}_{cGAN}(G, D) + \lambda \mathcal{L}_{L1}(G)$$

$$\mathcal{L}_{cGAN}(G, D) = \mathbb{E}_{x,y}[\log D(x, y)] + \mathbb{E}_{x,z}[\log(1 - D(x, G(x, z)))]$$

$$\mathcal{L}_{L1}(G) = \mathbb{E}_{x,y,z}[\|y - G(x, z)\|_1]$$

PatchGAN



Figure 6: Patch size variations. Uncertainty in the output manifests itself differently for different loss functions. Uncertain regions become blurry and desaturated under L1. The 1×1 PixelGAN encourages greater color diversity but has no effect on spatial statistics. The 16×16 PatchGAN creates locally sharp results, but also leads to tiling artifacts beyond the scale it can observe. The 70×70 PatchGAN forces outputs that are sharp, even if incorrect, in both the spatial and spectral (colorfulness) dimensions. The full 286×286 ImageGAN produces results that are visually similar to the 70×70 PatchGAN, but somewhat lower quality according to our FCN-score metric (Table 3). Please see <https://phillipi.github.io/pix2pix/> for additional examples.

Image-to-Image Translation with Conditional Adversarial Networks (CVPR 2017)

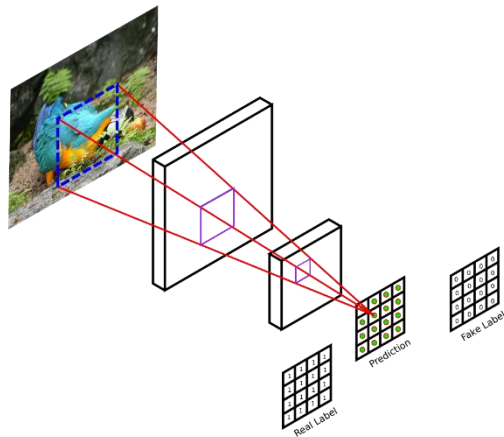
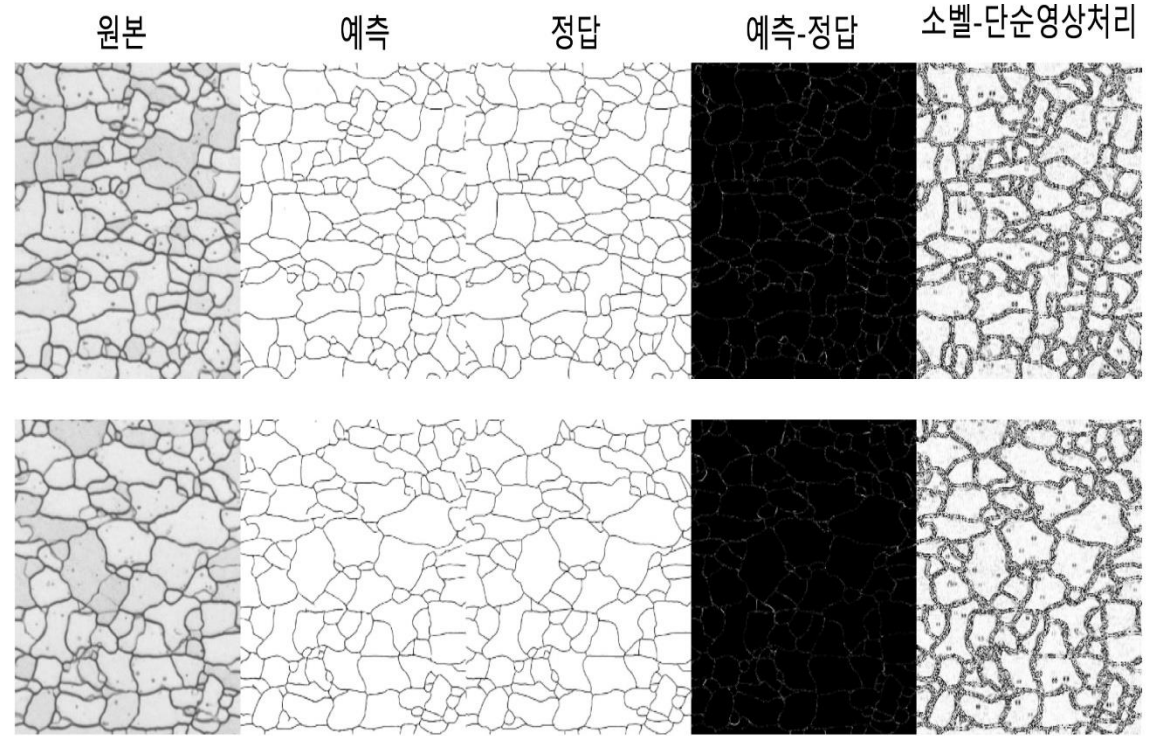
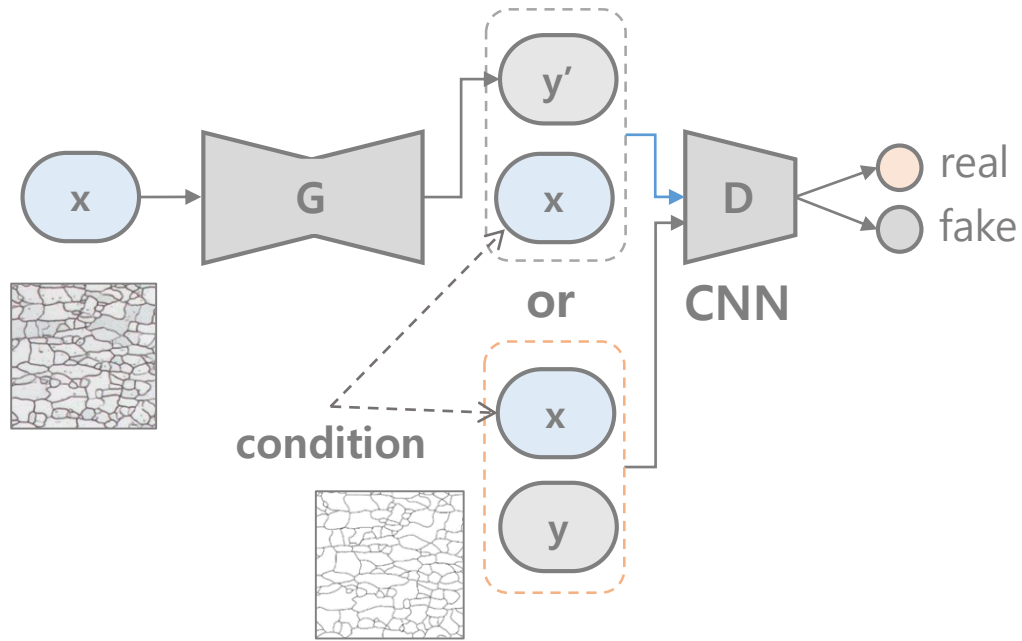


Figure 1: PatchGAN discriminator. Each value of the output matrix represents the probability of whether the corresponding image patch is real or it is artificially generated.

<https://arxiv.org/abs/1803.07422>

윤곽영상생성



생성자로,
RISA 적용 개선 U-Net 사용
SOTA 구조 적용

- Inception Module, Residual Block,
- Xception (depth-wise separable convolution)

CycleGAN

Unpaired Image-to-Image Translation

Using Cycle-Consistent Adversarial Networks (ICCV 2017)

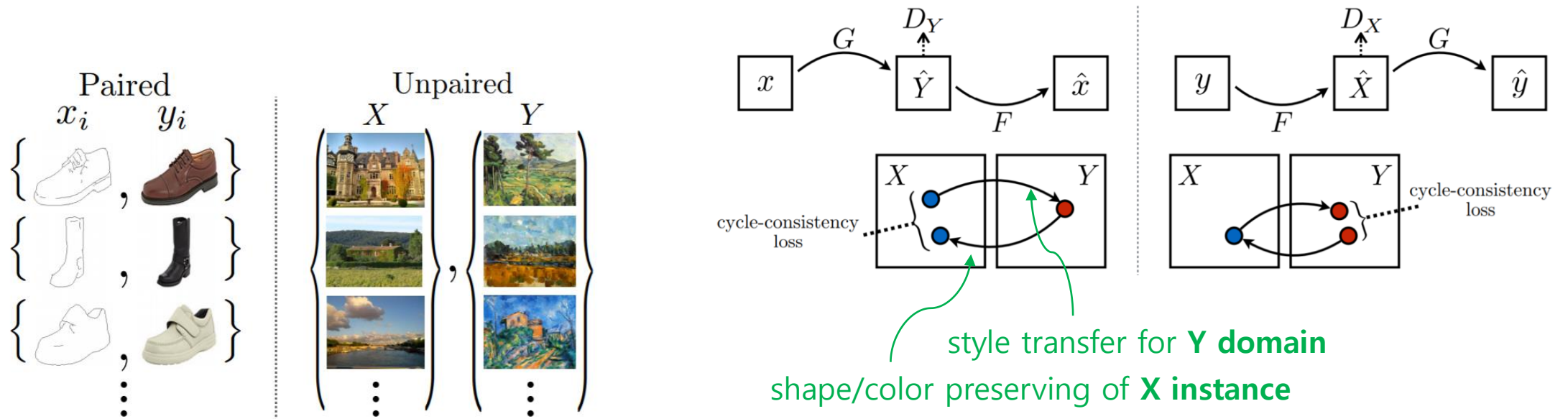


Figure 2: *Paired* training data (left) consists of training examples $\{x_i, y_i\}_{i=1}^N$, where the correspondence between x_i and y_i exists [21]. We instead consider *unpaired* training data (right), consisting of a source set $\{x_i\}_{i=1}^N$ ($x_i \in X$) and a target set $\{y_j\}_{j=1}^N$ ($y_j \in Y$), with no information provided as to which x_i matches which y_j .

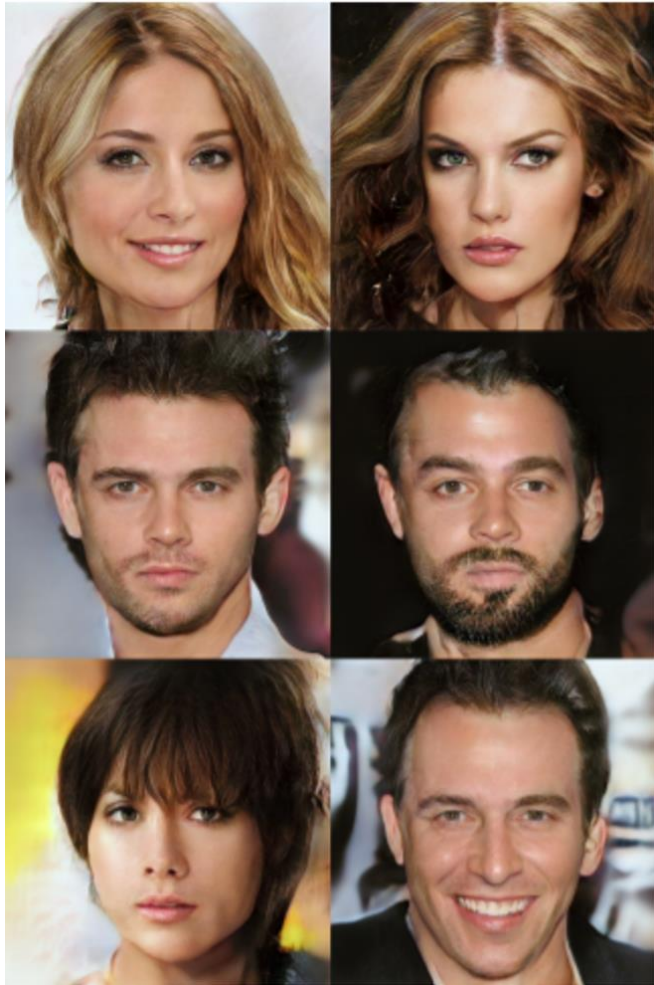
$$Loss_{x \rightarrow y} = \mathbb{E}_y[\log(D_y(y))] + \mathbb{E}_x[\log(1 - D_y(G(x)))] + \mathbb{E}_x[\|F(G(x)) - x\|_1]$$

$$Loss_{y \rightarrow x} = \mathbb{E}_x[\log(D_x(x))] + \mathbb{E}_y[\log(1 - D_x(F(y)))] + \mathbb{E}_y[\|G(F(y)) - y\|_1]$$

$$Loss_{cycleGAN} = Loss_{x \rightarrow y} + Loss_{y \rightarrow x}$$

NVidia

ProgressiveGAN(2017)



StyleGAN(2018)

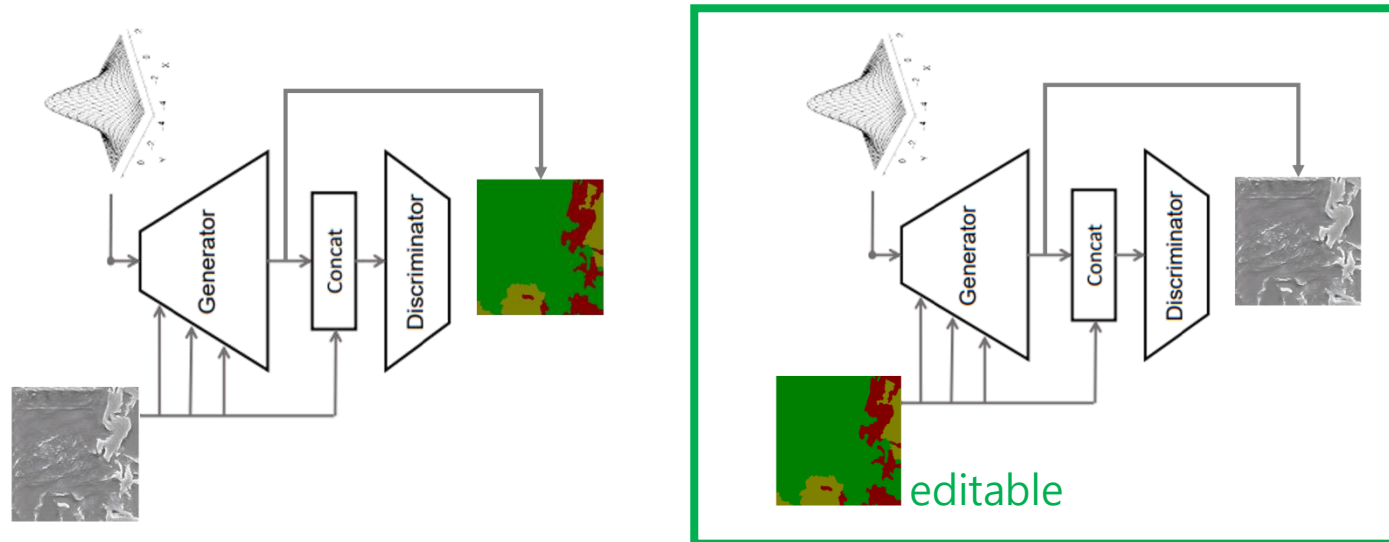
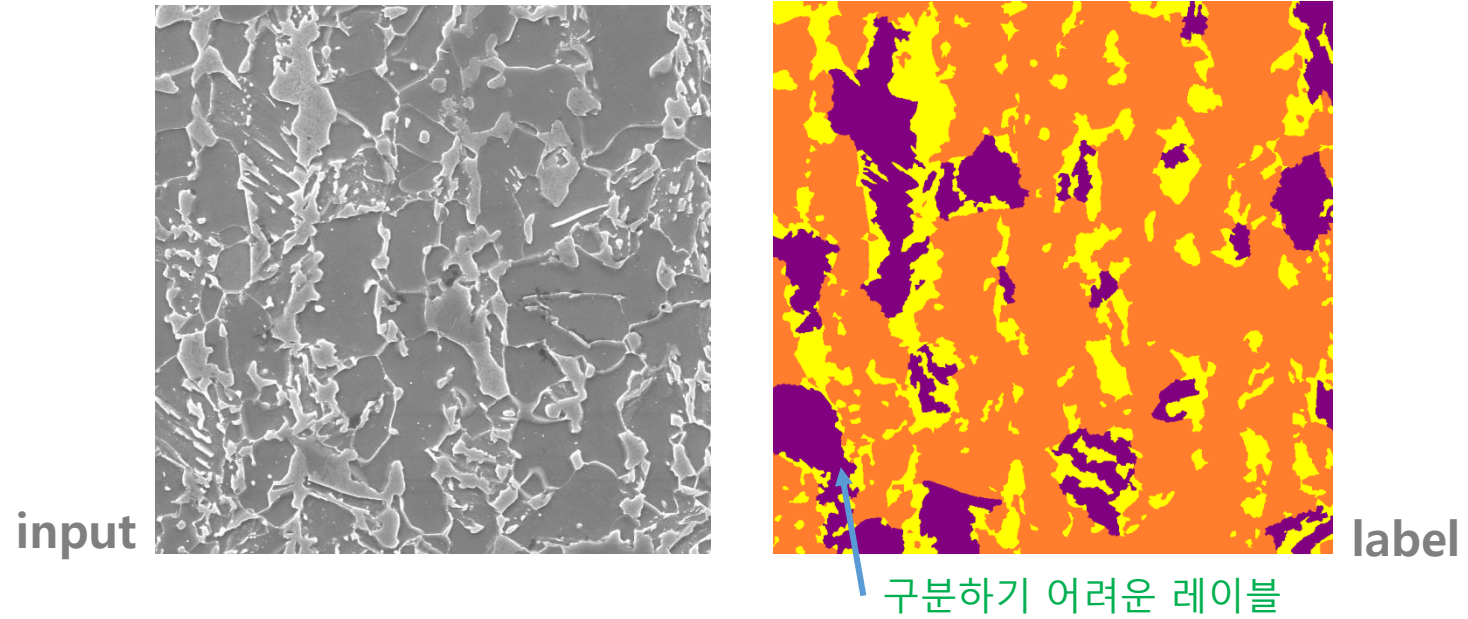


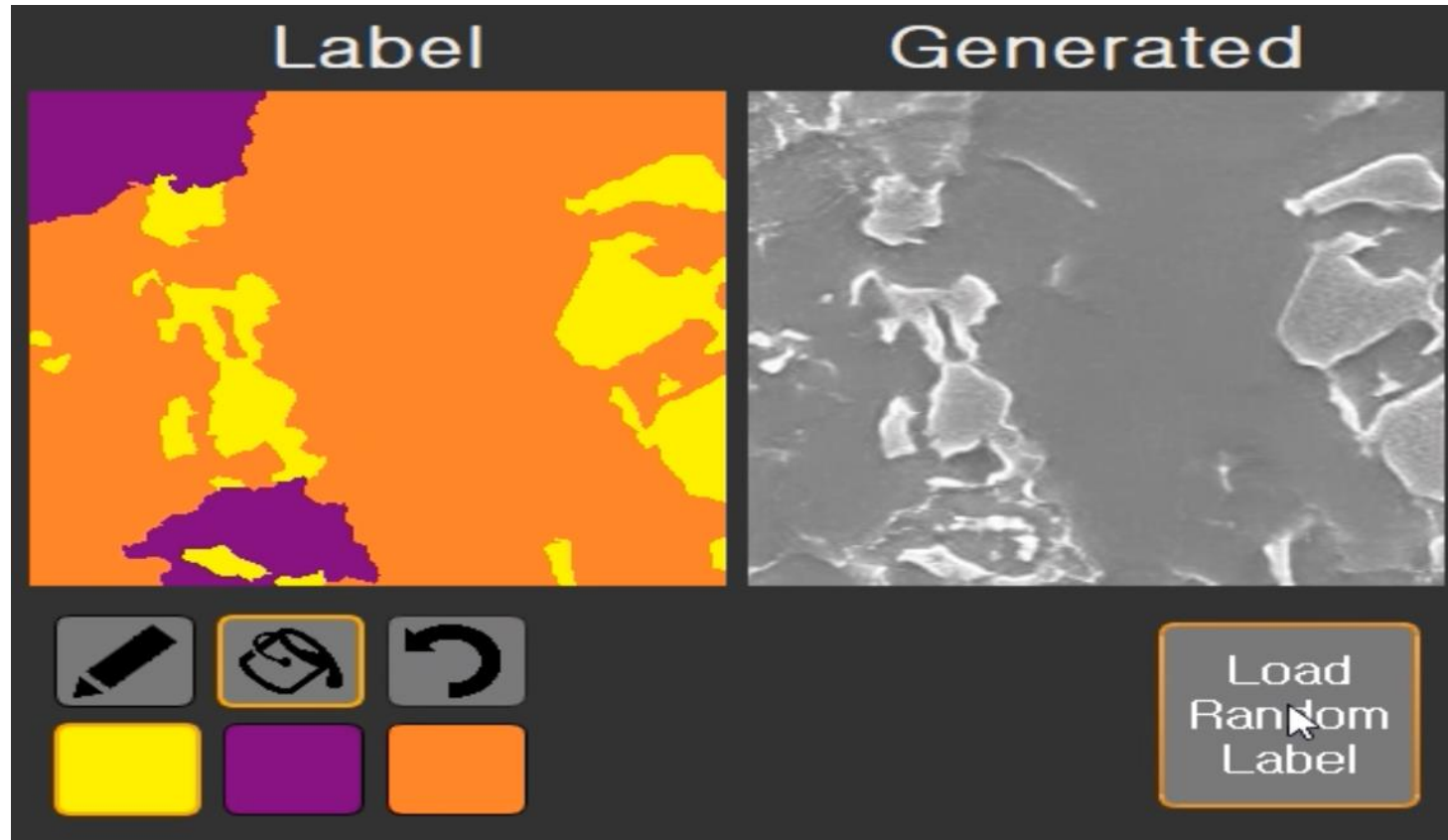
StyleGAN2(2020)



<https://developer.nvidia.com/blog/synthesizing-high-resolution-images-with-stylegan2/>

Label-Image Pair Generation





감사합니다.

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